

RAYLEIGH -TAYLOR INDUCED FRACTAL MIXING AND INTERMITTENCY

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Abstract

Scaled experiments on the nonlinear Rayleigh–Taylor (RT) front advance instability is described. First, at high Reynolds number, the mixing layer is found to grow self-similarly in a quadratic law. For a constant acceleration and as a power law, for an impulsive acceleration, $g = U_0 \delta(t)$. The growth coefficients α_i and exponents θ_i correspond to Richtmyer-Meshkov instability. Both conditions have been measured over a range of Atwood numbers A , both with Newtonian and more complex materials, the critical wavelength and amplitude for RT instability associated with the shear modulus and tensile yield of the material is varied for several conditions. The results may also be applied to naturally occurring supernova explosions, sediment overturning or volcanic islands. The role of local turbulence is studied and different experiments were compared using advanced visualization to analyse the fractal and multi-scale instabilities leading to mixing due to Rayleigh- Taylor and Richtmyer-Meshkov instabilities [1-3]. The evaluation of the scale to scale multifractal analysis in a finite-range-scale of the plume concentration images at different experimental conditions (the height of the source H), where the measure is the gray value of the image was applied to study its structure in time. The multifractal spectrum showed the characteristic inverse U shape and a similar evolution. At early times, the spectrum width was narrow with a left hand asymmetry evolving to a wider spectrum with a right asymmetry. The variation of the Hölder exponent ($\Delta\alpha$) presents different amplitudes increasing with time. The symmetry of the spectrum (Δf) decreases monotonically to an asymptotic value. The

multifractal spectrum and the parameters derived from this study can be used in transfer of energy and other descriptors of mixing, such as higher order structure function analysis in combination with Extended Self Similarity [6-8]. In particular we present the evolution of fluxes as molecular mixing takes place using fast reactive indicators such as Phenofalein, which provides 3D visual indication of the complexity of shock and buoyancy driven flows. We present a practical application in order to compare shocks Although the shock interaction process is inherently compressible, Richtmyer–Meshkov instability can be produced [7,8] The physical mechanism producing the instability is easily done [3] with the sudden stop of a tank in a falling frame of reference with vertical railing. We can resolve 2D velocities in a LIF plane or image sequence in mixing produced by either Rayleigh-Taylor instability, Richtmyer-Meshkov Instability or Kelvin-Helmholtz billows. Even when viscosities are small the two fluids are stirred and interpenetrating each other developing initially mushroomtype structures that degenerate into extremely thin and twisted filaments [3-6], even the large Reynolds number flows keep some memory of the intermittent forcing..The relationship between stratification, intermittency, $D(Ri)$ the fractal dimension of the flows and the turbulence energy spectral slope b , may be related [18-20]. For example the local measurements of dispersion, are related to the second order velocity moments, the skewness and kurtosis, etc. are related to asymmetry and intermittency, and so on. Analysis from conditional statistics of the relationship between maximum fractal dimension and buoyancy $D(Ri)$ [6] for stable flows have been confirmed and are also extended to unstable flows.

Both the laboratory experiments and the 2D-3D aspects of the turbulence cascade are much more complicated than first believed. The use of models comparing the corresponding relative scaling exponents estimated from more than two characteristic parameters (D , b). Then it is possible to find parameters at higher orders (p) of scaling exponents $D(p)$ and $b(p)$ obtained in a similar way as in [5]. It is not possible to perform an analysis independently on the initial conditions, neither for the RM nor for the RT flows. Therefore, the choice and classification of mixing descriptors has to consider the initial fields. The contour plots of the vorticity structures in general are smoother and exhibit lower fractal the physical space present than those of scalar mixing or volume fraction. To extend the measurements to complex flows a pattern matching technique was developed. This technique utilises similar method and its parameters as markers of shocks, the $f(\alpha)$ - α curves are similar to the ones obtained from energy dissipation fields which are influenced by the velocity gradients at the viscous scales The similar $f(\alpha)$ - α curves might imply that the flow

structure in the RT turbulent flow maximizes the entropy of the structure [11].

Each multifractal parameter obtained in each photogram marking the evolution at all the heights within the experiment. However, the curves describing the experiment, but the gaps in the flow seem due mainly to the lower values presented in the algorithms found by DigiFlow in PIV and in synthetic schlieren [4]. This allows the highly accurate pattern matching algorithms developed for synthetic schlieren to produce a local velocity field. The boundary condition effects and the role of combining the topological 3D and 2D characteristics of the individual flows relate to the scale to scale turbulent and inverse cascades. An important consideration apparent in the evaluation of the intermittency and the multi-fractal dimensions. is that velocity, vorticity and volume-fraction or scalar concentration exhibit different scaling laws [5,10]. This highlights the need for further comparisons to numerical simulations with different initial conditions, and detailed experiments, which is an important issue to understand the properties of mixtures and to relate them to geometric (multi-fractal) and dynamical mixing properties of the flows.[9-11]

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